

Datatype-Generic Programming in Haskell

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(thanks to José Pedro Magalhães, Simon Peyton Jones and many others)

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Datatypes are great

- ▶ Easy to introduce.
- ▶ Distinguished from existing types by the compiler.
- ▶ Added safety.
- ▶ Can use domain-specific names for types and constructors.
- ▶ Quite readable.

Datatypes are not so great

- ▶ New datatypes have no associated library.
- ▶ Cannot be compared for equality, cannot be (de)serialized, cannot be traversed, ...

Fortunately, there is **deriving** .

Derivable classes

In Haskell 2010:

Eq , Ord , Enum , Bounded , Read , Show

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Eq , Ord , Enum , Bounded , Read , Show

In GHC (in addition to the ones above):

Functor , Traversable , Typeable , Data , Generic

What about other classes?

For many additional classes, we can intuitively derive instances.

But can we also do it in practice?

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But can we also do it in practice?

Options:

- ▶ use an external preprocessor,
- ▶ use Template Haskell,
- ▶ use `data-derive`,
- ▶ or use the GHC **Generic** support.

From the user perspective:

Step 1

Define a new datatype and derive `Generic` for it.

```
data MyType a b =  
  Flag Bool | Combo (a, a) | Other b Int (MyType a a)  
deriving Generic
```


From the user perspective:

Step 2

Use a library that makes use of GHC **Generic** and give an empty instance declaration for a suitable type class:

```
import Data.Binary
```

```
...
```

```
instance (Binary a, Binary b)  $\Rightarrow$  Binary (MyType a b)
```

Analyzing **deriving**

Equality as an example

```
class Eq' a where  
  eq :: a → a → Bool
```

Let's define some instances by hand.

Equality on binary trees

```
data T = L | N T T
```

```
instance Eq' T where
```

```
  eq L      L      = True
```

```
  eq (N x1 y1) (N x2 y2) = eq x1 x2 && eq y1 y2
```

```
  eq _      _      = False
```

Equality on another type

```
data Choice = I Int | C Char | B Choice Bool | S Choice
```

Equality on another type

```
data Choice = I Int | C Char | B Choice Bool | S Choice
```

Assuming instances for `Int`, `Char`, `Bool`:

```
instance Eq' Choice where
```

```
  eq (I n1    ) (I n2    ) = eq n1 n2
```

```
  eq (C c1    ) (C c2    ) = eq c1 c2
```

```
  eq (B x1 b1) (B x2 b2) = eq x1 x2 &&  
                               eq b1 b2
```

```
  eq (S x1    ) (S x2    ) = eq x1 x2
```

```
  eq _        _          = False
```

What is the pattern?

- ▶ How many cases does the function definition have?
- ▶ What is on the right hand sides?

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Relevant concepts:

- ▶ number of constructors in datatype,
- ▶ number of fields per constructor,
- ▶ recursion leads to recursion,
- ▶ other types lead to invocation of equality on those types.

More datatypes

```
data Tree a = Leaf a | Node (Tree a) (Tree a)
```

Like before, but with labels in the leaves.

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data Tree a = Leaf a | Node (Tree a) (Tree a)
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Like before, but with labels in the leaves.

```
instance Eq' a  $\Rightarrow$  Eq' (Tree a) where
```

```
  eq (Leaf n1    ) (Leaf n2    ) = eq n1 n2
```

```
  eq (Node x1 y1) (Node x2 y2) = eq x1 x2 && eq y1 y2
```

```
  eq _           _           = False
```

Yet another equality function

This is often called a **rose tree**:

```
data Rose a = Fork a [Rose a]
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Assuming an instance for lists:

```
instance Eq' a  $\Rightarrow$  Eq' (Rose a) where  
  eq (Fork x1 xs1) (Fork x2 xs2) = eq x1 x2 && eq xs1 xs2
```

- ▶ Parameterization of types is reflected by parameterization of the functions (via constraints on the instances).
- ▶ Using parameterized types in other types then works as expected.

The equality pattern

An informal description

In order to define equality for a datatype:

- ▶ introduce a parameter for each parameter of the datatype,
- ▶ introduce a case for each constructor of the datatype,
- ▶ introduce a final catch-all case returning `False`,
- ▶ for each of the other cases, compare the constructor fields pair-wise and combine them using `(&&)`,
- ▶ for each field, use the appropriate equality instance.

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- ▶ for each field, use the appropriate equality instance.

If we can describe it, [can we write a program to do it?](#)

Interlude:
type isomorphisms

Isomorphism between types

Two types **A** and **B** are called **isomorphic** if we have functions

$$f :: A \rightarrow B$$
$$g :: B \rightarrow A$$

that are mutual **inverses**, i.e., if

$$f \circ g \equiv \text{id}$$
$$g \circ f \equiv \text{id}$$

Example

Lists and Snoc-lists are isomorphic

```
data SnocList a = Lin | SnocList a :> a
```

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Lists and Snoc-lists are isomorphic

```
data SnocList a = Lin | SnocList a :> a
```

```
listToSnocList :: [a] → SnocList a
```

```
listToSnocList [] = Lin
```

```
listToSnocList (x : xs) = listToSnocList xs :> x
```

```
snocListToList :: SnocList a → [a]
```

```
snocListToList Lin = []
```

```
snocListToList (xs :> x ) = x : snocListToList xs
```

We can (but won't) prove that these are inverses.

The idea of datatype-generic programming

- ▶ Represent a type `A` as an isomorphic type `Rep A`.

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- ▶ Represent a type `A` as an isomorphic type `Rep A`.
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The idea of datatype-generic programming

- ▶ Represent a type `A` as an isomorphic type `Rep A`.
- ▶ If a limited number of type constructors is used to build `Rep A`,
- ▶ then functions defined on each of these type constructors
- ▶ can be lifted to work on the original type `A`
- ▶ and thus on any representable type.

Choice between constructors

Which type best encodes choice between constructors?

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data Either a b = Left a | Right b
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```
data Either a b = Left a | Right b
```

Choice between three things:

```
type Either3 a b c = Either a (Either b c)
```

Combining constructor fields

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```
data (a, b) = (a, b)
```

Combining three fields:

```
type Triple a b c = (a, (b, c))
```

What about constructors without arguments?

We need another type.

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```
data () = ()
```

Representing types

Representing types

To keep representation and original types apart, let's define isomorphic copies of the types we need:

```
data U      = U
data a :+: b = L a | R b
data a **: b = a **: b
```

Representing types

To keep representation and original types apart, let's define isomorphic copies of the types we need:

```
data U      = U
data a :+: b = L a | R b
data a **: b = a **: b
```

We can now get started:

```
data Bool = False | True
```

How do we represent `Bool` ?

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data a **: b = a **: b
```

We can now get started:

```
data Bool = False | True
```

How do we represent `Bool` ?

```
type RepBool = U :+: U
```

A class for representable types

```
class Generic a where
```

```
  type Rep a
```

```
  from :: a → Rep a
```

```
  to   :: Rep a → a
```

The type `Rep` is an associated type.

A class for representable types

```
class Generic a where
```

```
  type Rep a
```

```
  from :: a → Rep a
```

```
  to   :: Rep a → a
```

The type `Rep` is an [associated type](#).

Equivalent to defining `Rep` separately as a [type family](#):

```
type family Rep a
```

Representable Booleans

```
instance Generic Bool where  
  type Rep Bool = U :+: U  
  from False = L U  
  from True  = R U  
  to   (L U) = False  
  to   (R U) = True
```

Representable lists

```
instance Generic [a] where  
  type Rep [a] = U :+: (a :+: [a])  
  from []           = L U  
  from (x : xs)    = R (x :+: xs)  
  to (L U          ) = []  
  to (R (x :+: xs)) = x : xs
```

Representable lists

```
instance Generic [a] where  
  type Rep [a] = U :+: (a :+: [a])  
  from []           = L U  
  from (x : xs)    = R (x :+: xs)  
  to (L U          ) = []  
  to (R (x :+: xs)) = x : xs
```

Note:

- ▶ shallow transformation,
- ▶ no constraint on `Generic a` required.

Representable trees

```
instance Generic (Tree a) where  
  type Rep (Tree a) = a :+: (Tree a :* Tree a)  
  from (Leaf n      ) = L n  
  from (Node x y    ) = R (x :* y)  
  to   (L n         ) = Leaf n  
  to   (R (x :* y)) = Node x y
```

Representable rose trees

```
instance Generic (Rose a) where  
  type Rep (Rose a) = a :*: [Rose a]  
  from (Fork x xs) = x :*: xs  
  to   (x :*: xs ) = Fork x xs
```


Representing primitive types

We don't ...

Back to equality

Intermediate summary

- ▶ We have defined class `Generic` that maps datatypes to representations built up from `U`, `(:+:)`, `(:*:)` and other datatypes.
- ▶ If we can define equality on the representation types, then we should be able to obtain a generic equality function.
- ▶ Let us apply the informal recipe from earlier.

A class for generic equality

```
class GEq a where  
  geq :: a → a → Bool
```

Instance for sums

instance (GEq a, GEq b) \Rightarrow GEq (a :+: b) **where**

geq (L a₁) (L a₂) = geq a₁ a₂

geq (R b₁) (R b₂) = geq b₁ b₂

geq _ _ = False

Instance for products and unit

```
instance (GEq a, GEq b)  $\Rightarrow$  GEq (a :: b) where  
  geq (a1 :: b1) (a2 :: b2) = geq a1 a2 && geq b1 b2  
instance GEq U where  
  geq U U = True
```

Instances for primitive types

```
instance GEq Int where  
  geq = ((=) :: Int → Int → Bool)
```

What now?

Dispatching to the representation type

```
defaultEq :: (Generic a, GEq (Rep a)) => a -> a -> Bool
defaultEq x y = geq (from x) (from y)
```

Dispatching to the representation type

```
defaultEq :: (Generic a, GEq (Rep a)) => a -> a -> Bool
defaultEq x y = geq (from x) (from y)
```

Defining generic instances is now trivial:

```
instance GEq Bool where
  geq = defaultEq
instance GEq a => GEq [a] where
  geq = defaultEq
instance GEq a => GEq (Tree a) where
  geq = defaultEq
instance GEq a => GEq (Rose a) where
  geq = defaultEq
```

Dispatching to the representation type

```
defaultEq :: (Generic a, GEq (Rep a)) => a -> a -> Bool
defaultEq x y = geq (from x) (from y)
```

Or with the DefaultSignatures language extension:

```
class GEq a where
  geq :: a -> a -> Bool
  default geq :: (Generic a, GEq (Rep a)) => a -> a -> Bool
  geq = defaultEq

instance GEq Bool
instance GEq a => GEq [a]
instance GEq a => GEq (Tree a)
instance GEq a => GEq (Rose a)
```

Isn't this as bad as before?

Question

Haven't we just replaced some tedious work (defining equality for a type) by some other tedious work (defining a representation for a type)?

Amount of work

Question

Haven't we just replaced some tedious work (defining equality for a type) by some other tedious work (defining a representation for a type)?

Yes, but:

- ▶ The representation has to be given only once, and works for potentially many generic functions.
- ▶ Since there is a single representation per type, it could be generated automatically by some other means (compiler support, TH).
- ▶ In other words, it's sufficient if we can use **deriving** on class `Generic`.

So can we derive **Generic**?

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Yes (with `DeriveGeneric`) ...

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Yes (with `DeriveGeneric`) ...

...but the representations are not quite as simple as we've pretended before:

```
class Generic a where  
  type Rep a  
  from :: a → Rep a  
  to   :: Rep a → a
```

So can we derive **Generic**?

Yes (with `DeriveGeneric`) ...

...but the representations are not quite as simple as we've pretended before:

```
class Generic a where  
  type Rep a :: * → *  
  from :: a → Rep a x  
  to   :: Rep a x → a
```

Representation types are actually of kind `* → *`.

An extra argument?

- ▶ It's a pragmatic choice.
- ▶ Facilitates some things, because we also want to derive classes parameterized by type constructors (such as `Functor`).
- ▶ For now, let's just try to “ignore” the extra argument.

Simple vs. GHC representation

Old:

```
type instance Rep (Tree a) = a :+: (Tree a **: Tree a)
```

New:

```
type instance Rep (Tree a) =  
  M1 D D1Tree  
    (M1 C C1_0Tree  
      (M1 S NoSelector (K1 P a))  
      :+:  
      M1 C C1_1Tree  
        (M1 S NoSelector (K1 R (Tree a))  
          **:  
          M1 S NoSelector (K1 R (Tree a))  
        )  
    )  
  )
```

Simple vs. GHC representation

Old:

```
type instance Rep (Tree a) = a :+: (Tree a :+: Tree a)
```

New:

```
type instance Rep (Tree a) =
```

```
    :+:
      (
        :+:
          )
      a
      Tree a
      Tree a
```

Familiar components

Everything is now lifted to kind $* \rightarrow *$:

```
data U1      a = U1
data (f :+ : g) a = L1 (f a) | R1 (g a)
data (f :* : g) a = f a :* : g a
```

Wrapping constant types

This is an extra type constructor wrapping every constant type:

```
newtype K1 t c a = K1 {unK1 :: c}
data P    -- marks parameters
data R    -- marks other occurrences
```

The first argument **t** is not used on the right hand side. It is supposed to be instantiated with either **P** or **R**.

```
newtype M1 t i f a = M1 {unM1 :: f a}
data D    -- marks datatypes
data C    -- marks constructors
data S    -- marks (record) selectors
```

Depending on the tag `t`, the position `i` is to be filled with a datatype belonging to class `Datatype`, `Constructor`, or `Selector`.


```
class Datatype d where  
  datatypeName :: w d f a → String  
  moduleName   :: w d f a → String
```

Meta information – contd.

```
class Datatype d where  
  datatypeName :: w d f a → String  
  moduleName   :: w d f a → String
```

```
instance Datatype D1Tree where  
  datatypeName _ = "Tree"  
  moduleName   _ = ...
```

Similarly for constructors.

Adapting the equality class(es)

Works on representation types:

```
class GEq' f where  
  geq' :: f a → f a → Bool
```

Works on “normal” types:

```
class GEq a where  
  geq :: a → a → Bool  
  default geq :: (Generic a, GEq' (Rep a)) ⇒ a → a → Bool  
  geq x y = geq' (from x) (from y)
```

Instance for `GEq Int` and other primitive types as before.

Adapting the equality class(es) – contd.

instance (GEq' f, GEq' g) \Rightarrow GEq' (f :+: g) **where**

geq' (L1 x) (L1 y) = geq' x y

geq' (R1 x) (R1 y) = geq' x y

geq' _ _ = False

Similarly for `:::` and `U1`.

Adapting the equality class(es) – contd.

instance (GEq' f, GEq' g) \Rightarrow GEq' (f :+: g) **where**

geq' (L1 x) (L1 y) = geq' x y

geq' (R1 x) (R1 y) = geq' x y

geq' _ _ = False

Similarly for `:*:` and `U1` .

An instance for constant types:

instance GEq a \Rightarrow GEq' (K1 t a) **where**

geq' (K1 x) (K1 y) = geq x y

Adapting the equality classes – contd.

For equality, we ignore all meta information:

```
instance GEq' f  $\Rightarrow$  GEq' (M1 t i f) where  
  geq' (M1 x) (M1 y) = geq' x y
```

All meta information is grouped under a single datatype, so that we can easily ignore it all if we want to.

Adapting the equality classes – contd.

For equality, we ignore all meta information:

```
instance GEq' f  $\Rightarrow$  GEq' (M1 t i f) where  
  geq' (M1 x) (M1 y) = geq' x y
```

All meta information is grouped under a single datatype, so that we can easily ignore it all if we want to.

Functions such as `show` and `read` can be implemented generically by accessing meta information.

Constructor classes

To cover classes such as `Functor`, `Traversable`, `Foldable` generically, we need a way to map between a type `constructor` and its representation:

```
class Generic1 f where  
  type Rep1 f :: * -> *  
  from1 :: f a -> Rep1 f a  
  to1   :: Rep1 f a -> f a
```

Use the same representation type constructors, plus

```
data Par1 p   = Par1 {unPar1 :: p }  
data Rec1 f p = Rec1 {unRec1 :: f p }
```

GHC from version 7.6 is able to derive `Generic1`, too.

Conclusions

- ▶ For more examples, look at `generic-deriving`.
- ▶ As a user of libraries, less boilerplate, easy to use.
- ▶ Safer (but less powerful) than Template Haskell.
- ▶ As a library author: consider using this!

Thank you – Questions?

Extra slides

Template Haskell

- ▶ Has the full syntax tree. Can do much more.
- ▶ You have to do more work to derive using TH.
- ▶ It's trickier to get it right. Corner cases. Name manipulation.
- ▶ Datatype-generic functions are type-checked.
- ▶ Uniform interface to the user.
- ▶ Admittedly, allowing **deriving** would be even easier.

- ▶ Similar ideas.
- ▶ Need other representations.
- ▶ Except for SYB, no direct GHC support.
- ▶ But we can convert! (ICFP 2013 submission)